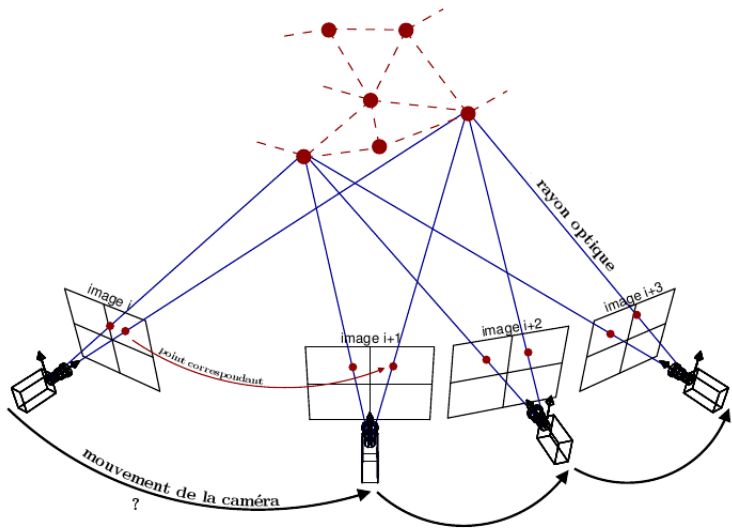


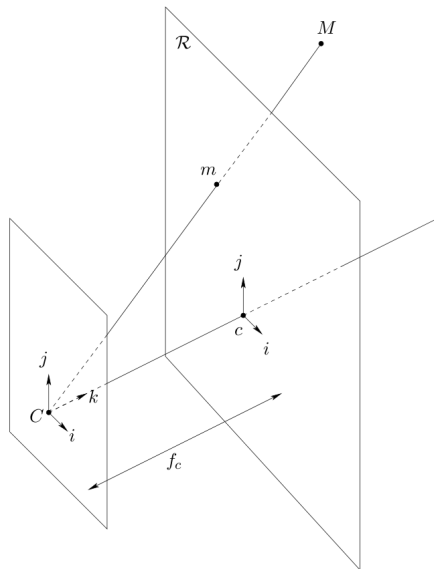
Estimation of a video sequence camera motion

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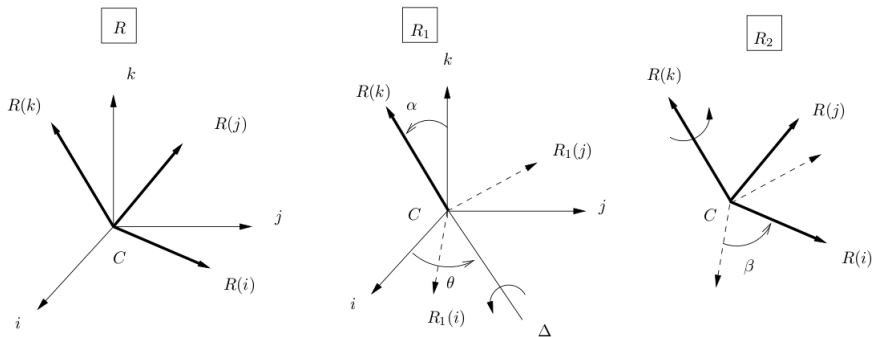


Pinhole camera model



Motion decomposition and parameterization

$R = R_2 \circ R_1$ is parametrized by (θ, α, β) :



$\tilde{t} := \frac{t}{Z_0} = (-A, -B, -C)$ in $(R(i), R(j), R(k))$.

From now on, $\Theta = (\theta, \alpha, \beta, A, B, C)$.

Optical flow approximation

For a unitary focal length

$$\begin{cases} x' = \frac{r_{1,1}x + r_{2,1}y + r_{3,1} - \left\langle \frac{t}{Z(x,y)}, R(i) \right\rangle}{r_{1,3}x + r_{2,3}y + r_{3,3} - \left\langle \frac{t}{Z(x,y)}, R(k) \right\rangle} \\ y' = \frac{r_{1,2}x + r_{2,2}y + r_{3,2} - \left\langle \frac{t}{Z(x,y)}, R(j) \right\rangle}{r_{1,3}x + r_{2,3}y + r_{3,3} - \left\langle \frac{t}{Z(x,y)}, R(k) \right\rangle} \end{cases}$$

Under three hypotheses, the more limiting one being a quasi-constant depth:

$$\begin{pmatrix} x' - x \\ y' - y \end{pmatrix} \simeq \begin{pmatrix} A - \alpha \sin \theta \\ B + \alpha \cos \theta \end{pmatrix} + \begin{pmatrix} -C & \beta \\ -\beta & -C \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} -\alpha \sin \theta & \alpha \cos \theta & 0 \\ 0 & -\alpha \sin \theta & \alpha \cos \theta \end{pmatrix} \begin{pmatrix} x^2 \\ xy \\ y^2 \end{pmatrix}$$

A differential algorithm

Minimization over Θ of the quantity $\sum_{(x,y) \in S} (u_{\Theta}(x,y) - u(x,y))^2$.

u_{Θ} is linear in $(c_1, c_2, a_1, a_2, q_1, q_2)$, where

$$c_1 = A - \alpha \sin \theta$$

$$c_2 = B + \alpha \cos \theta$$

$$a_1 = -C$$

$$a_2 = \beta$$

$$q_1 = -\alpha \sin \theta$$

$$q_2 = \alpha \cos \theta$$

We use a classical least-square method using in input an optical flow computed by Horn-Schunk method.

Jonchéry's algorithm

Jonchéry's idea: minimize in mean over Θ the quantity

$$DF_{\Theta, \xi}(x, y) = g((x, y) + u_{\Theta}(x, y)) - f(x, y) + \xi$$

Incremental scheme:

$$(\Theta_{k+1}, \xi_{k+1}) = (\Theta_k, \xi_k) + (\Delta\Theta_k, \Delta\xi_k)$$

Limited development at first order:

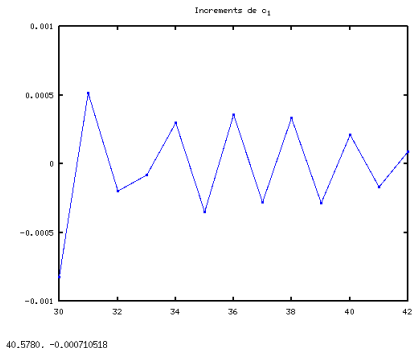
$$DF_{\Theta_{k+1}, \xi_{k+1}} \simeq r_{\Delta\Theta_k, \Delta\xi_k} := DF_{\Theta_k, \xi_k}(x, y) + \nabla g((x, y) + u_{\Theta_k}(x, y)) \cdot u_{\Delta\Theta_k}(x, y) + \Delta\xi_k$$

Computation of $(\Delta\Theta_k, \Delta\xi_k)$: minimization of the quantity

$$\sum_{(x, y) \in \mathcal{S}} r_{\Delta\Theta_k, \Delta\xi_k}^2$$

Stopping criterion

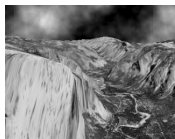
The increments oscillate after enough iterations:



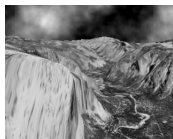
At step N , we stop the iterations if $\left| \sum_{k=N-5}^N \Delta a_{1k} \right| \leq \frac{|\Delta a_{1N} - \Delta a_{1N-1}|}{2}$.

Experimentations

- Scenes satisfying the hypotheses
- Scenes with two depth plans
- Scenes with a small object in movement
- Textures
- Scenes with many depths



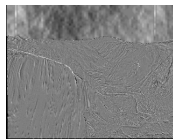
I_1



I_2



Optical flow



Warped difference

Comparison between the two algorithms

- Running times are equivalent.

Pair of images	Jonchéry's algorithm	Differential algorithm
baboon	1,01	0,91
vcbox	4,25	1,32
pepsi-complete	0,60	0,65
street	1,30	0,57
fortuny	2,74	4,57
urban	5,56	4,26
homography	2,24	0,99
pluto	9,70	29,04

Table: Running times in seconds

- However, Jonchéry's algorithm can adress larger motions.

	θ	α	β	A	B	C
Expected	any	0	$8.73 \cdot 10^{-2}$	0	0	0
Jonchéry	2.06	$1.55 \cdot 10^{-4}$	$8.65 \cdot 10^{-2}$	$3.60 \cdot 10^{-4}$	$-6.70 \cdot 10^{-5}$	$7.57 \cdot 10^{-3}$
Differential	4.12	$8.021 \cdot 10^{-2}$	$7.96 \cdot 10^{-2}$	$-7.39 \cdot 10^{-2}$	$4.50 \cdot 10^{-2}$	$3.07 \cdot 10^{-2}$

Table: Result of the algorithms for a rotation of 5 degrees



B.K. Horn and B.G. Shunk.
Determining optical flow.
Artificial Intelligence, 1981.



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Estimation d'un mouvement de caméra et problèmes connexes.
PhD thesis, ENS Cachan, 2007.



Enric Meinhardt-Llopis and Javier Sánchez Pérez.
Horn-schunk optical flow with a multi-scale strategy.
IPOLE, 2001.



M.R Osborne.
Finite algorithms in optimization and data analysis.
John Wiley, 1985.